

Interference and the Wave Nature of Light

Interference:

Constructive Interference: two identical waves arrive at a point in phase and reinforce each other

Destructive Interference: two identical waves arrive at a point out of phase and cancel each other

⇒ two waves that are initially in phase can arrive at a point out of phase if they travel different distances

$$\text{constructive interference: } \Delta L = L_2 - L_1 = m\lambda \quad m = 0, 1, 2, \dots$$

$$\text{destructive interference: } \Delta L = L_2 - L_1 = (m + 1/2)\lambda \quad m = 0, 1, 2, \dots$$

Young's Double-Slit Experiment:

$$\text{bright fringes: } \sin \theta = \frac{m\lambda}{d} \quad m = 0, 1, 2, \dots \quad \text{dark fringes: } \sin \theta = \frac{(m + 1/2)\lambda}{d} \quad m = 0, 1, 2, \dots$$

⇒ use $y = L \tan \theta$ to find the distance between the fringes

Thin Film Interference:

⇒ the wavelength that is important is the wavelength within the film: $\lambda_{\text{film}} = \frac{\lambda_{\text{vacuum}}}{n_{\text{film}}}$

⇒ there is a $\frac{1}{2} \lambda$ phase change when light reflects from a region with a higher index of refraction

⇒ if only one of the waves undergoes a $\frac{1}{2} \lambda$ phase change:

$$\text{constructive interference: } 2t = (m + 1/2)\lambda_{\text{film}} \quad m = 0, 1, 2, \dots$$

$$\text{destructive interference: } 2t = m\lambda_{\text{film}} \quad m = 0, 1, 2, \dots$$

⇒ if neither of the waves or if both waves undergo a $\frac{1}{2} \lambda$ phase change:

$$\text{constructive interference: } 2t = m\lambda_{\text{film}} \quad m = 0, 1, 2, \dots$$

$$\text{destructive interference: } 2t = (m + 1/2)\lambda_{\text{film}} \quad m = 0, 1, 2, \dots$$

Diffraction:

$$\text{dark fringes for single-slit diffraction: } \sin \theta = \frac{m\lambda}{W} \quad m = 1, 2, 3, \dots$$